

Name: \_\_\_\_\_

Date: \_\_\_\_\_

## M12P HW Section 7.3 Solving Exponential Equations and Basic Logarithm

$$a^x \times a^y = a^{x+y} \qquad a^m \div a^n = a^{m-n} \qquad \left(a^m\right)^n = a^{m \times n} \qquad a^y \times b^y = (ab)^y$$

1. When you multiply two powers with the same base, do you “add” or “multiply” their exponents? Explain
2. What is the difference between:  $(-a)^4$  vs  $-a^4$
3. What is the purpose of logarithm? How would you use logarithms to find the value of “x”:  $a^x = b$
4. How would you use logarithm to find the value of “x”?  $6^x = 120$ . Show your work:
5. Is there a solution to the equation? Explain:  $3^x = -1$
6. How would you solve this problem? Can you use logarithm? Explain:  $(-2)^x = -131072$
7. How about his next problem, how would you solve it using logarithm?  $(-2)^x = -1048576$

8. Solve the following equations using basic exponential rules: Show all your work and steps:

|   |                           |                           |
|---|---------------------------|---------------------------|
| a) $3^{x+1} = 81$                         | b) $4^{x-2} = 64$         | c) $9^{x+1} = 2173$       |
| d) $16^x = 65536$                         | e) $8 \times 2^5 = 2^x$   | f) $\frac{27}{3^2} = 3^x$ |
| g) $\left(\frac{512}{2^5}\right)^2 = 2^x$ | h) $243 = \frac{3^x}{27}$ | i) $12^x = 2^6 3^3$       |
| j) $\frac{64}{2^x} = 1024$                | k) $(27)^3 = 3^x$         | l) $3^{2x} = 729$         |
| m) $4^{3x} = 128$                         | n) $729^x = 81$           | o) $4^{x+1} = 65536$      |

|   |  |  |
|---|--|--|
| p) $25^{2x} = 78125$  | q) $36^{x+3} = 7776$   | r) $4^x (16) = 64$   |
| s) $(3^{2x})^3 = 81$  | t) $\frac{16^x}{2^{3x}} = 128$                                 | u) $(4^{x+1})(2^5) = 65536$  |
| v) $\frac{(729^x)^3}{9^{x-3}} = 3$                                    | w) $\left(\frac{8^{-1} + 2^{-3}}{4^{-3}}\right)^3 = 32^{-x+1}$ | x) $12^4 = 2^x 3^y$  |
| y) $\left(\frac{81^{x+4}}{9^5}\right)^4 = \left(\frac{1}{3}\right)^x$ | z) $\left(\frac{16^{-x}}{32^2}\right)^4 = 64^{x+1}$            | ii) $\left(\frac{(81^2)9^x}{729^3}\right)^{-1} = \frac{(3^{3x+1})}{9^x}$ |

9. Solve the following equations by factoring:

$$a) 9^x - 30(3^x) + 81 = 0$$

$$b) 16^x - 12(4^x) + 32 = 0$$

$$c) (8)^{2x} - 18(8)^x + 32 = 0$$

$$d) 16^x - 10(2^{2x+2}) + 256 = 0$$

$$e) 12(9^x) - 17(3^x) + 6 = 0$$

$$f) 15(25^x) - 41(5^x) = -14$$

$$g) 56(4^{x-1}) - 6(2^{x-1}) = 5$$

$$h) 3(9^{x+1}) - 8(3^{x+1}) + 4 = 0$$

